

Development of statistical methods for DNA copy number analysis in cancerology

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Outline

- 1 Introduction
- 2 Segmentation
- 3 Heterogeneity Model
- 4 Simulations
- 5 Application to real data sets
- 6 Conclusion

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- 1 Introduction
 - Alterations in tumor cells
 - Notion of Heterogeneity
- 2 Segmentation
- 3 Heterogeneity Model
- 4 Simulations
- 5 Application to real data sets
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Objectives

Alterations in tumor cells can be observed at several levels

- Gene expression
- DNA structure
- Mutations
- DNA copy number

Why study genetic alterations in cancers ?

- Help to diagnosis
- Identify biomarkers linked to drug resistance
- Personalized treatments

Objectives

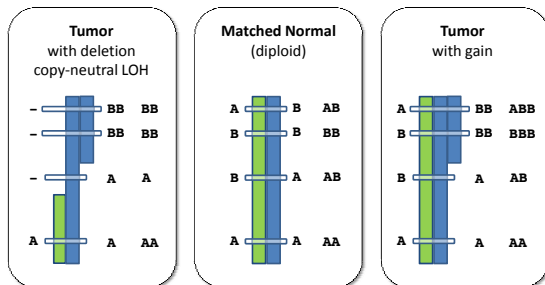
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- **DNA copy number**

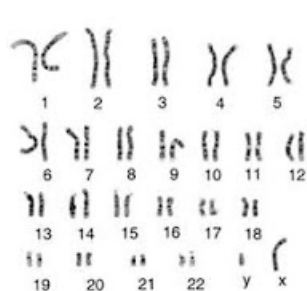
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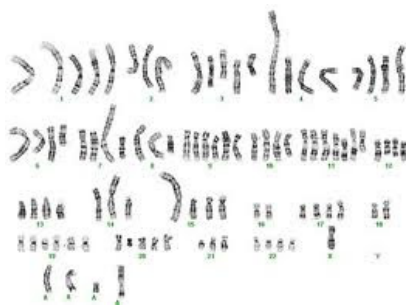
Illustration of alterations at level of DNA copy number



Human Karyotype



(a) Normal cell



(b) Tumor cell

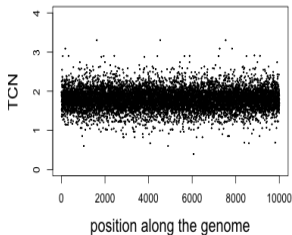
How to measure DNA copy number more precisely ?

- CGH arrays (measuring total DNA copy number)
- SNP arrays (measuring quantity of alleles for predefined SNPs)
- Sequencing technologies (WGS or WES)

What kind of signals from SNPs arrays?

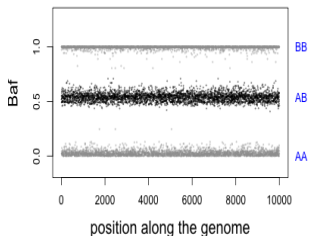
Total copy number

$$c_j = N_j^A + N_j^B$$



B allele fraction

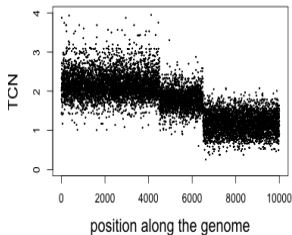
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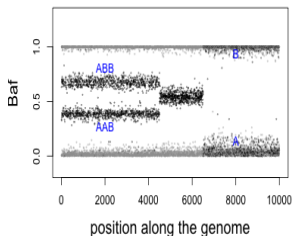
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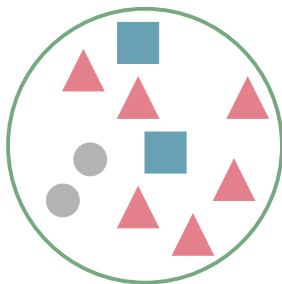
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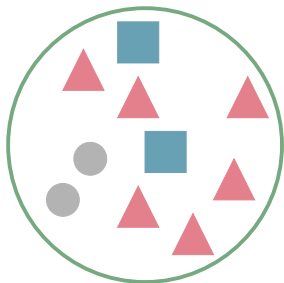
Notion of heterogeneity in cancers

- Differences between tumors of the same disease in different patients (inter-tumor heterogeneity)
- Differences between cancer cells within a single tumor of one patient (intra-tumor heterogeneity).

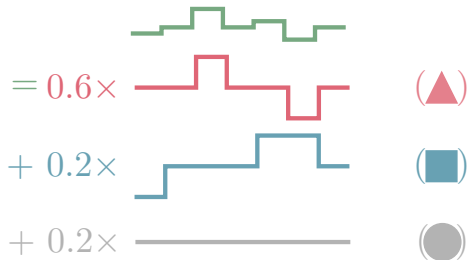


Heterogeneity illustration

(a) Tumor sample

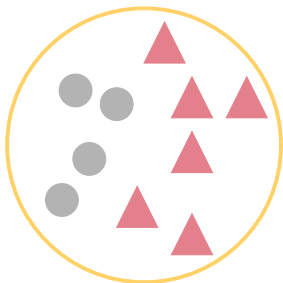


(b) Copy-number profile



Heterogeneity illustration

(a) Tumor sample



(b) Copy-number profile



Mathematical modelization

- $y_{1\bullet} \in \mathbb{R}^J$ and $y_{2\bullet} \in \mathbb{R}^J$ the observed DNA copy number profiles

$$y_{1\bullet} = w_{11}z_{1\bullet} + w_{12}z_{2\bullet} + w_{13}z_{3\bullet}$$

$$y_{2\bullet} = w_{21}z_{1\bullet} + w_{22}z_{2\bullet} + w_{23}z_{3\bullet}$$



- Find w and z for the two profiles

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- Find w and z for the two profiles

General mathematical modeling

- Let $y_{i\bullet} \in \mathbb{R}^J$ the **observed** DNA copy number profiles

$$y_{i\bullet} = \sum_{k=1}^p w_{ik} z_{k\bullet} + \epsilon$$

- Latent profiles assumed to be shared between the observed profiles

- Minimize $\sum_{i=1}^n \left\| y_{i\bullet} - \sum_{k=1}^p w_{ik} z_{k\bullet} \right\|^2$ under some constraints.

Related works

- Matrix Factorization problem

$$\min_{W,Z} \|Y - WZ\|_F^2$$

- Penalized latent models to infer heterogeneity
 - Fused Lasso latent model FL1at (Nowak et al., 2011)
 - CGH analysis with Dictionary Learning e-FL1at (Masecchia et al., 2013)
 - Evolutionary history by next-generation sequencing Canopy (Jiang et al., 2016)

InCaSCN- Inferring Cancer Subclone using Copy Number

Features of method

- joint segmentation of all n profiles $\Rightarrow S - 1$ breakpoints (Pierre-Jean et al., Briefings in Bioinformatics, 2015)
- Integration of B allele fraction information by using transformations
- Biological interpretation of constraints on latent profiles of TCN and BAF and weight matrix W

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 - Recursive Binary Segmentation for multiple samples
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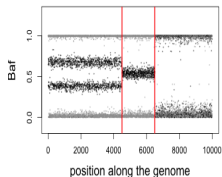
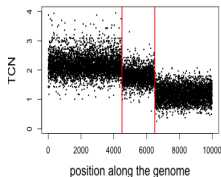
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B allele fraction

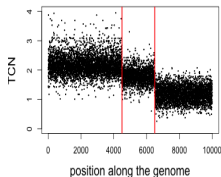
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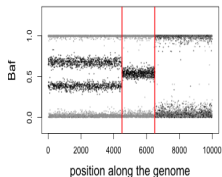
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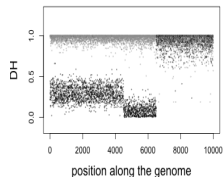
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Decrease of Heterozygosity

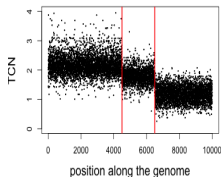
$$d_j = 2 \times |b_j - \frac{1}{2}|$$



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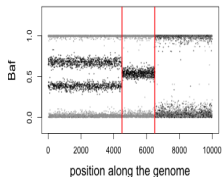
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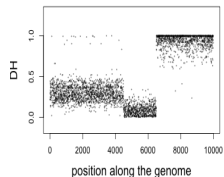
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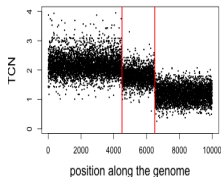
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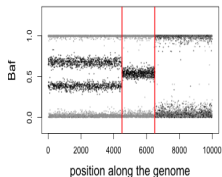
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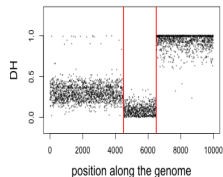
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Segmentation methods

- Multiple change-point
- Recursive

- Total variation
- Hidden Markov Models
- Kernel methods

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- Multiple change-point
- **Recursive**
 - **Joint segmentation**
- Total variation
- Hidden Markov Models
- Kernel methods
 - Change-point detection in whole distribution

A change-point model

- Biological assumption : DNA copy number signal is piecewise constant in the mean
- Statistical model for $S - 1$ change points at (t_1, \dots, t_{S-1}) :

$$\forall j = 1, \dots, J \quad c_j = \gamma_j + \epsilon_j$$

where $\forall s \in \{1, \dots, S\}, \forall j \in [t_{s-1}, t_s[\quad \gamma_j = \Gamma_s$

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Complexity

- Challenges : S and (t_1, \dots, t_{S-1}) are unknown
- For a fixed S , the number of possible partitions :

$$C_{J-1}^{S-1} = \mathcal{O}(J^{S-2})$$

Two-step approaches for joint segmentation

Gey and Lebarbier (2008) and Vert and Bleakley (2010)

First step :

- Running a **fast** but **approximate** segmentation method (RBS)

Second step

- Pruning the final set of breakpoints using dynamic programming that is **slower** but **exact**

Versatility of RBS

- Possibility to have different scales
- TCN-DoH segmentation
- Several TCN signals
- Several TCN-DoH signals

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Binary Segmentation

- Take the simple case : dimension is equal to 1 ($d = 1$) :
- \mathcal{H}_0 : No breakpoint vs \mathcal{H}_1 : Exactly one breakpoint
- The likelihood ratio statistic is given by $\max_{1 \leq j \leq J} |Z_j|$

$$Z_j = \frac{\left(\frac{S_j}{j} - \frac{S_J - S_j}{J-j} \right)}{\sqrt{\frac{1}{j} + \frac{1}{J-j}}}, \quad (1)$$

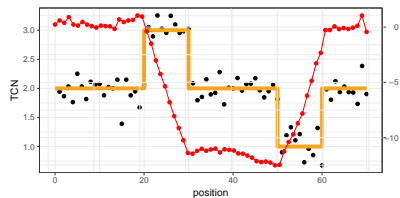
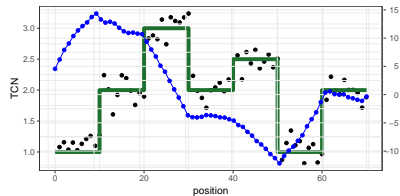
And $S_j = \sum_{1 \leq t \leq j} c_j$

If ($d > 1$) : the likelihood ratio statistic becomes $\max_{1 \leq j \leq J} \|Z_j\|_2^2$

First step : Recursive Binary Segmentation (RBS)

Complexity : $O(dJ \log(S))$

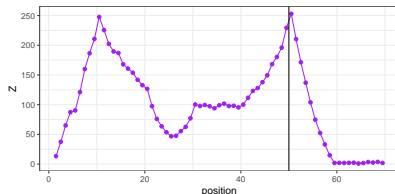
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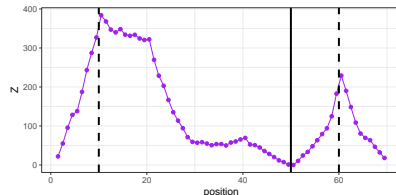
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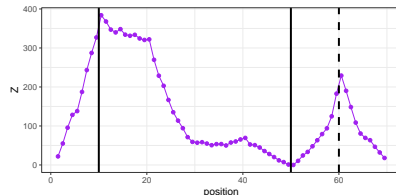
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- Second breakpoint :
 - $\max_{1 \leq j \leq t_1} \|Z_j\|_2^2$
 - $\max_{t_1 < j \leq J} \|Z_j\|_2^2$
- Compute RSE for each segment.
- Keep the RSE that yield the maximum gain
- Add the breakpoint to the active set



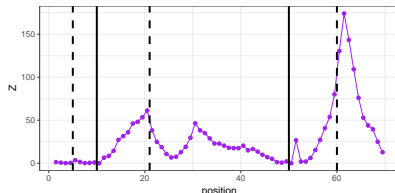
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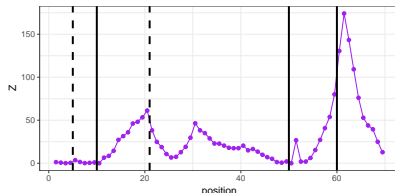
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- Third breakpoint :
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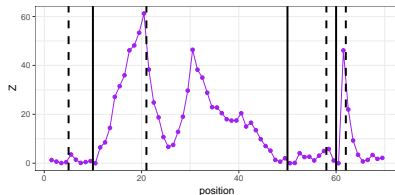
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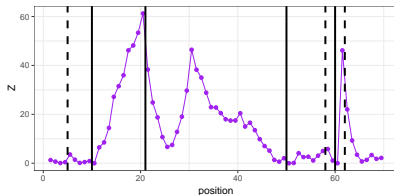
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Summary

Contributions to segmentation methods

- Implementation of a fast joint segmentation followed by a pruning. (jointseg package)
- Kernel methods (preprint submitted to CSDA)
- Evaluation of performance (Pierre-Jean et al., Briefings in Bioinformatics, 2015)

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 - Model
 - Algorithm
 - Model selection
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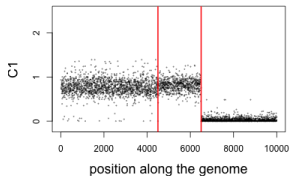
Integrating BAF through Parental copy numbers

What is parental copy number ?

$d_j = 2|b_j - 1/2|$ for AB SNPs

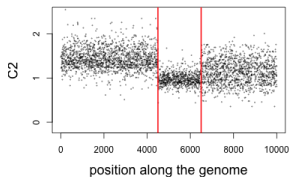
Minor copy number

$$c_j^1 = c_j(1 - d_j)/2$$



Major copy number

$$c_j^2 = c_j(1 + d_j)/2$$



Model on parental copy number

$$\min_{W, Z^1, Z^2} \|Y^1 - WZ^1\|_F^2 + \lambda_1 \sum_{k=1}^p \sum_{s=1}^{S-1} |z_{k,s+1}^1 - z_{k,s}^1| \quad (2)$$

$$\|Y^2 - WZ^2\|_F^2 + \lambda_2 \sum_{k=1}^p \sum_{s=1}^{S-1} |z_{k,s+1}^2 - z_{k,s}^2|$$

s. t $w_{j\bullet} \in \Delta_p$ where

$$\Delta_p = \left\{ w \in \mathbb{R}^p \quad \text{s.t.} \quad w \geq 0 \quad \text{and} \quad \sum_{k=1}^p w_k = 1 \right\}$$

Final algorithm

Algorithm 1 Find weights and latent profiles

- 1: **Parameters** : λ_1, λ_2 and p
 - 2: **INIT** : Matrices $Y \in \mathbb{R}^{n \times S}$, $Y^1 \in \mathbb{R}^{n \times S}$ and $Y^2 \in \mathbb{R}^{n \times S}$ and matrix Z_0^1 and $Z_0^2 \in \mathbb{R}^{p \times S}$, and
 - 3: **for** $l = 0, 1, 2, \dots$ **do**
 - 4: Minimize in W with Z_l^1 and Z_l^2 fixed
 - 5: Minimize in Z^1 with W_l fixed
 - 6: Minimize in Z^2 with W_l fixed
 - 7: W_l, Z_l^1 and Z_l^2 are updated
 - 8: Check if $\|W_{l-1} - W_l\|_2^2 < \epsilon$ or max_{it} is reached
 - 9: **end for**
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Final algorithm

Algorithm 2 Find weights and latent profiles

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Solving 4 : Inference of W

- Weights of each patient can be treated independently
- Solve n least-squares problems with equality constraint plus inequality constraints for the non-negativity of the coefficient
- linear inverse problem that can be solved in R with the package **limSolve**.

Solving 5 and 6 : Inference of latent profiles

- for a fixed W cut into two independent LASSO problems in (Z_1, Z_2)
- Use matrix algebra and properties of the vectorization operator
- Obtain LASSO problem that can be solved in R with the package **glmnet**.

Choice of λ_1 and λ_2 values when p is fixed

- Use a BIC criterion
- We search to minimize :

$$(nS) \times \log \left(\frac{\|Y - \hat{W}\hat{Z}\|_F^2}{nS} \right) + k(Z) \log(nS)$$

where $k(Z^T)$ is the number of breakpoints.

- This criterion helps to strike a balance between over-fit and under-fit models.

Choice of p

- Use the percentage of variation explained (PVE) for each p , where the PVE is defined as :

$$PVE_p = 1 - \frac{\sum_{i=1}^n \sum_{j=1}^S (y_{ij} - \sum_{k=1}^p \hat{w}_{ik} \hat{z}_{kj})^2}{\sum_{i=1}^n \sum_{j=1}^S (y_{ij} - \bar{y}_i)^2}$$

where $\bar{y}_i = \frac{\sum_{j=1}^S y_{ij}}{S}$.

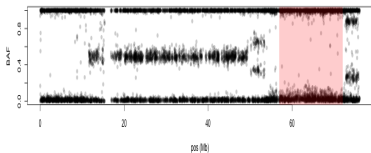
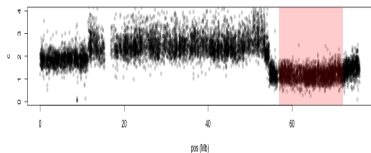
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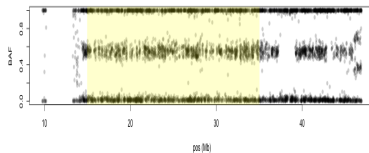
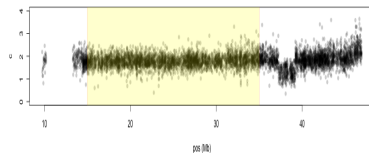
Proposed approach

Step 1- Annotate a real data set

Loss of one copy (Chr18)



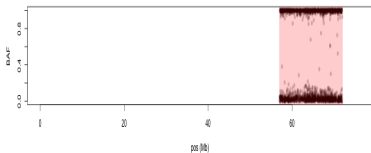
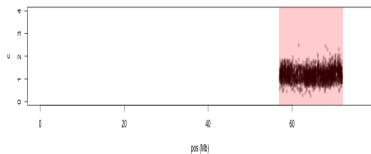
Normal region (Chr21)



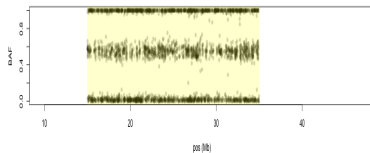
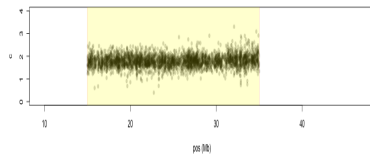
Proposed approach

Step 1- Annotate a real data set

Loss of one copy (Chr18)

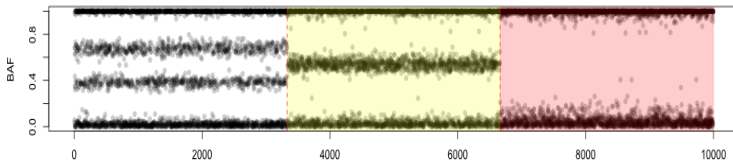
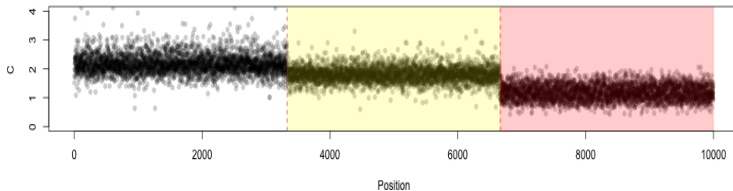


Normal region (Chr21)



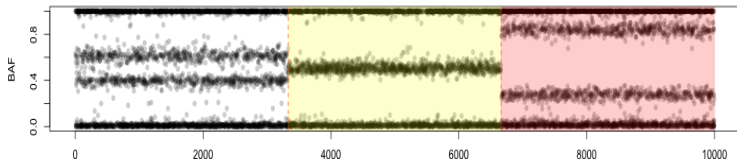
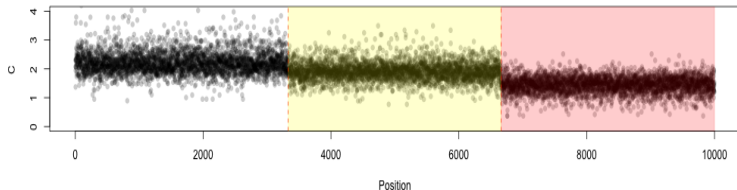
Proposed approach

Step 2 - Synthetic data generation by resampling 100% tumor cells



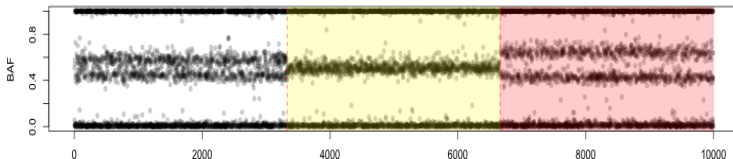
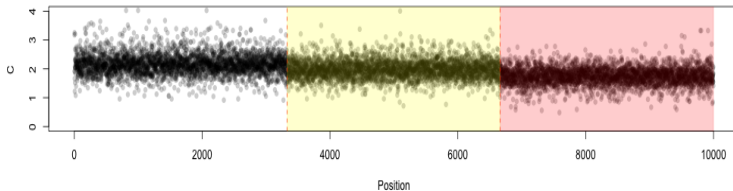
Proposed approach

Step 2 - Synthetic data generation by resampling 79% tumor cells



Proposed approach

Step 2 - Synthetic data generation by resampling 50% tumor cells



Summary

Advantages

- 1 More realistic noise Hocking et al. (2013)
- 2 SNR is controlled with the proportion of tumor cells Staaf et al. (2008); Rasmussen et al. (2011)
- 3 Variety of simulated profiles Willenbrock and Fridlyand (2005)
- 4 True and false positive evaluation Hocking et al. (2013)

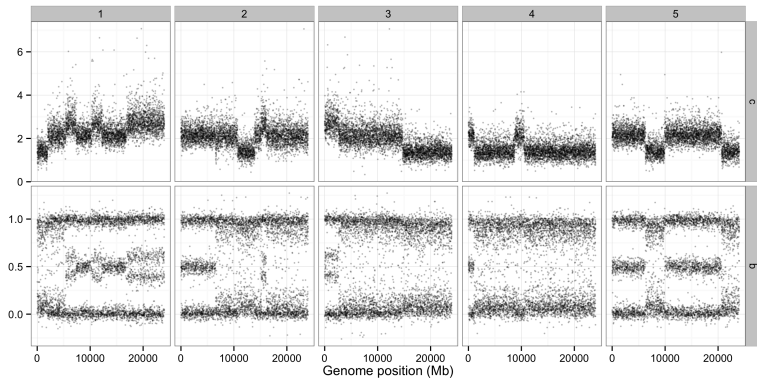
Application

- 1 Performance of segmentation methods
- 2 Evaluation of heterogeneity model

Characteristics

- 100 data sets simulated
- 30 tumor samples and 5 latent profiles based on realistic simulation framework
- Each matrix W is different for the 100 data sets

Simulated latent profiles

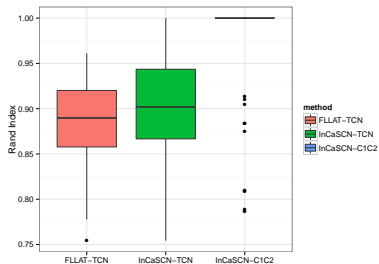
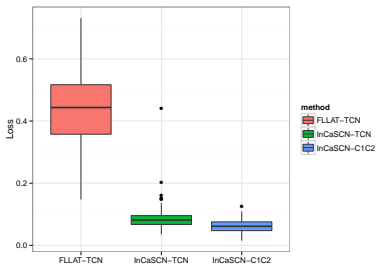


Performance evaluation

We compared performance of three methods :

- InCaSCN on parental copy number profiles
- InCaSCN on total copy number profiles
- FLLAT on total copy number profiles (Nowak et al., 2011)

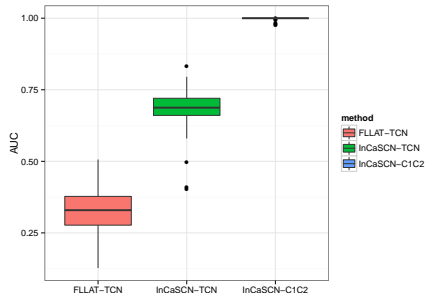
Better estimation and interpretation of weights by using InCaSCN



Inferred latent profiles from InCaSCN recover the true alterations

Evaluation

- Characterize each region as normal or altered for latent profiles
- AUC close to 1 : altered regions have been recovered with a few number of mistakes



Conclusion

- InCaSCN enables to recover both :
 - simulated latent profiles
 - weights with a small error
- Results on simulation are very promising for the application to real data sets.

Outline

- 1 Introduction
- 2 Segmentation
- 3 Heterogeneity Model
- 4 Simulations
- 5 Application to real data sets**
 - Inter-tumoral heterogeneity application
 - Intra-tumoral heterogeneity application
- 6 Conclusion

Collaboration with Institut Curie

- Fabien Reygal's team (RT² : Residual Tumor and Response to Treatment)
- Triple-negative breast cancer (TNBC)
 - 16 patients
 - Micro-biopsy of the Primary Tumor at diagnosis
 - Neo-adjuvant chemotherapy before surgery
 - Primary Tumor size reduced but incomplete → Residual
 - 10 patients with Primary Tumor and Residual samples
 - 6 patients with an additional metastasis Lymph Node sample
- Whole exome sequencing data
- RNAseq data

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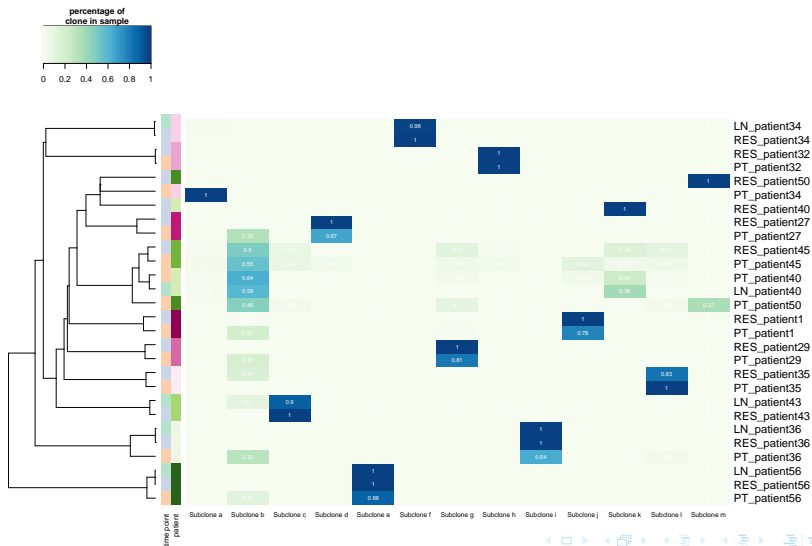
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Inter-tumoral heterogeneity application

Results



Conclusion on the application

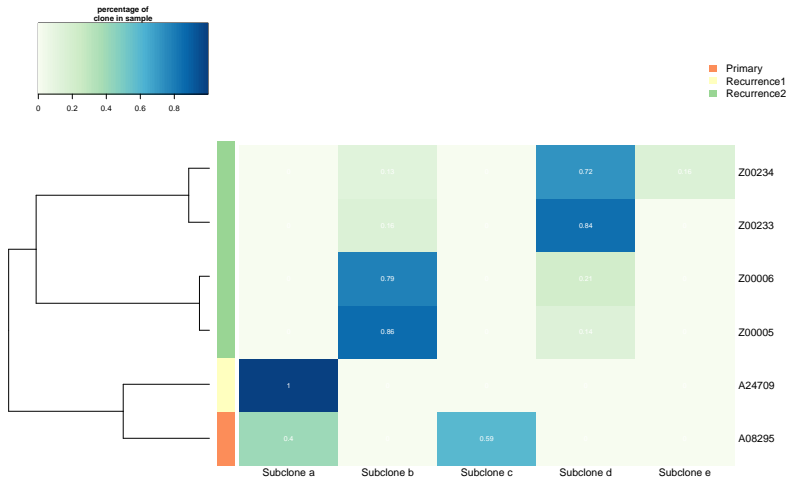
- Only one latent profile (subclone B) common across the patients
- Patients are mainly grouped together
- For two patients (40 and 50), it seems that the resistant clone is already present in PT and becomes largely predominant in RES
- Same results from RNAseq analysis (B. Sadacca)

Collaboration with UCSF

- Henrik Bengtsson and Joe Costello
- Glioblastoma
 - 96 patients
 - Primary Tumor samples
 - Recurrence 1 with several samples
 - Sometimes Recurrence 2 with several samples
- Whole exome sequencing data
- Preprocessing with sequenza

Intra-tumoral heterogeneity application

Results



Conclusions

Conclusions

- One resistant subclone already present in PT
- New cancer in Recurrence 2

Conclusions on the model

- Fast and efficient algorithm
- Application to other data sets
- Similar results than the model that uses mutations

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Contributions

- Segmentation Methods
- Realistic simulation framework
- Performance of segmentation methods
- Heterogeneity
- Bioinformatic pipelines under several R packages
 - jointseg
 - acnr
 - InCaSCN

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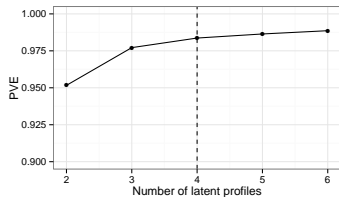
Perspectives

- Exploring DNA copy number latent profiles
- Link to clinical outcomes
- Discover biomarkers
- Collaboration with UCSF

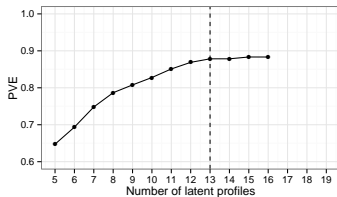
Thank you for your attention

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Selection of number of latent profiles



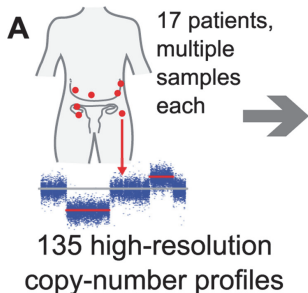
HSGOC



TNBCC

Intra-tumoral heterogeneity

- Public data set
- High serious grade ovarian cancer (HSGOC)

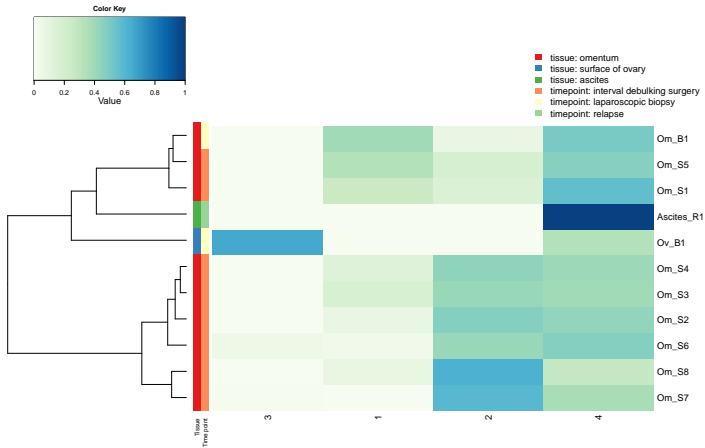


- Quantify heterogeneity
- Reconstruct tumor evolution

Results

- We focused on one patient with 11 samples
 - Ovary (Biopsy)
 - Omentum
 - Ascites (relapse)
- We select a model with 4 latent profiles

Results : Weight matrix



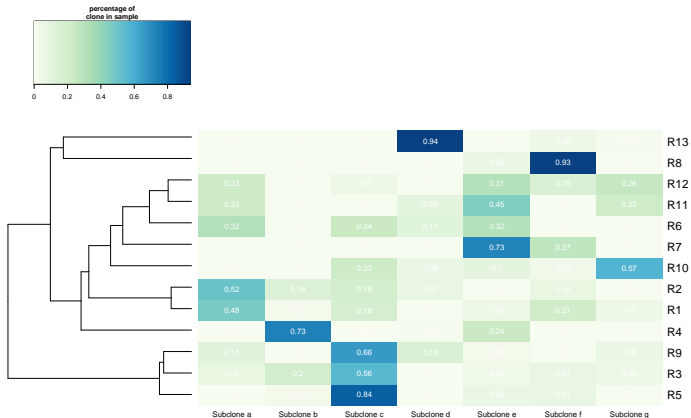
Conclusions an Perspectives

- One clone seems to be not resistant to the drug (latent profile 3)
- There may exist only one resistant clone to the drugs that led to a relapse (latent profile 4)
- exploring if there are not known genes that can be responsible for the resistance

Spatial Intra-tumoral heterogeneity

- Public data set
- Kidney cancer
- Several patients with several samples at various location.

Kidney cancer application



Sequencing information

- Illumina Hi-Seq 2500 pair-end aligned on hg19
- Depth : WEG : 100x
- bwa for alignment (soft clapping remove head and tail and map on the middle)
- reads sizes reads : 100 bases

Random Features

For a signal of length J .

Method	computation	Storage
Kernel	$\mathcal{O}(SJ^2)$	$\mathcal{O}(SJ)$
Approximation	$\mathcal{O}(p^2 J)$	$\mathcal{O}(SJ)$
Random Feature	$\mathcal{O}(SMJ)$	$\mathcal{O}(MJ)$